**Description:**

This element implements an attenuator using a resistor network. Three and Four terminals resistive attenuators are implemented. Four terminals must be specified in the netlist and the Three terminal implementation is used if the second and fourth terminals are the same.

The term attenuation, usually used in high frequency techniques, is defined as the ratio, expressed in decibels, of the power level or voltage level between two points in a circuit. The attenuation of a component under test will be the ratio, expressed in decibels, of the power absorbed by the load without the component in the line to the power absorbed by the load with the component in the line, when the signal source and the load are perfectly matched.

$$\text{Attenuation } A = 10 \log_{10} (P1/P2) \text{ db or } 10 \log_{10} (V1/V2) \text{ db}$$

P1 = power absorbed by the load without the component in the line

P2 = power absorbed by the load with the component in the line

V1 = input voltage

V2 = output voltage

Form:

attenuator:<instance name> n₁ n₂ n₃ n₄ <parameter list>

n₁ is the port #1 signal input terminal

n₂ is the port #1 reference terminal

n₃ is the port #2 signal output terminal

n₄ is the port #2 reference terminal (can be the same as n₂)

Parameters

Example

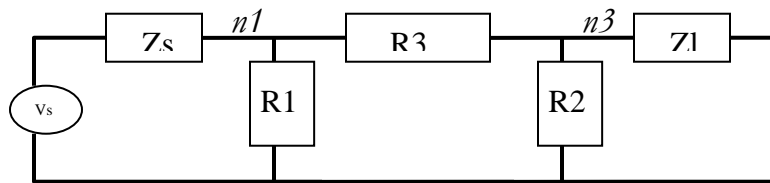
attenuator:a1 1 0 3 0 zo=50 alpha=2

attenuator:a1 1 0 3 4 zo=50 alpha=2

Parameter	Type	Default Value	Required?
Zo: characteristic impedance	DOUBLE	50	yes
alpha: attenuation constant	DOUBLE	N/A	yes

Model Documentation

Consider the following 3 terminal network when $n2=n4$ and derive the stamp:



Zs- source impedance

Zl- load impedance

Assuming $Zs=Zl = Zo$

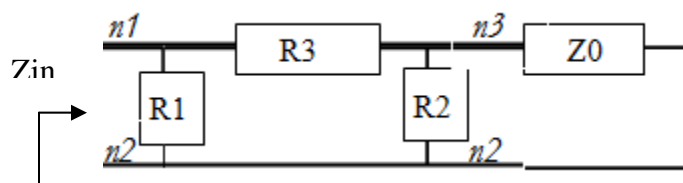


Fig.1

$$R1 \parallel (R3 + (R2 \parallel Z_o)) = Z_o \quad (\dots\dots a)$$

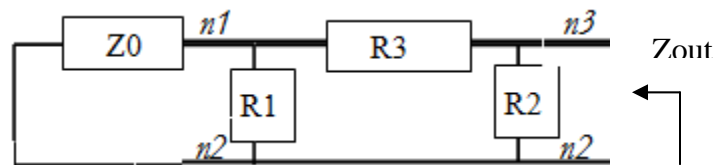


Fig.2

$$R2 \parallel (R3 + (R1 \parallel Z_o)) = Z_o \quad (\dots\dots b)$$

Solving 'a' and 'b' we get $R_1 = R_2$

Now

$$\alpha = 10 \log(P_1/P_2) \text{ db}$$

$$\text{where } P_1 = V_1^2/(2Z_o) \text{ and } P_2 = V_2^2/(2Z_o)$$

therefore

$$\alpha = 20 \log(V_1/V_2) \text{ db}$$

$$k = V_1/V_2 = 10 (\alpha/20) \quad (\dots\dots c)$$

Applying KCL at node n1 and n3:

$$V_1/Z_o = V_1/R_1 + (V_1 - V_2)/R_3 \quad (\dots\dots d)$$

$$(V_1 - V_2)/R_3 = V_2/R_2 + V_2/Z_o \quad (\dots\dots e)$$

Combining 'c' and 'd':

$$V_1/Z_o = V_1/R_1 + V_2/R_1 + V_2/Z_o \quad (\dots\dots f)$$

Eliminating V_2 and using equation 'c':

$$k-1/Z_o = k+1/R_1$$

$$\mathbf{R_1 = R_2 = Z_o(k+1)/(k-1)}$$

Using equation 'e':

$$\mathbf{R_3 = Z_o(k^2-1)/(2k)}$$

Therefore, $g_1 = 1/R_1$; $g_2 = 1/R_2$; $g_3 = 1/R_3$

We obtain the final stamp of the matrix as given below:

$$\begin{array}{c|ccc} & 1 & 2 & 3 \\ \hline 1 & g_1 + g_3 & -g_1 & -g_3 \\ 2 & -g_1 & g_1 + g_2 & -g_2 \\ 3 & -g_3 & -g_2 & g_2 + g_3 \end{array}$$

The stamp of the 4 terminal network is obtained on the similar lines as the 3 terminal network.

	1	2	3	4
1	$g_1 + g_3$	$-g_1$	$-g_3$	0
2	$-g_1$	$g_1 + g_4$	0	$-g_4$
3	$-g_3$	0	$g_2 + g_3$	$-g_2$
4	0	$-g_4$	$-g_2$	$g_2 + g_3$

$$g_1 = 1/R_1; g_2 = 1/R_2; g_3 = 1/R_3; g_4 = 1/R_4$$

$$R_1 = R_2 = Z_0(k+1)/(k-1)$$

$$R_3 = R_4 = Z_0(k^2-1)/(4k)$$

Version: 1

Credits:

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